Designing a Simple Loss Function for the Fed: Does the Dual Mandate Make Sense?

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DKLN (UPF, KU, Riksbank & Boston Fed) On the Design of Simple Mandates

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- Advances in academic research Rogoff (1985) and Persson and Tabellini (1993) supported a strong focus on price stability
 - As documented in Svensson (2010), many central banks became "inflation targeters" to strengthen credibility and facilitate accountability, setup of ECB one prominent example

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 - Woodford optimal mandate/loss function: $L_t = (\pi_t^a \pi^*)^2 + \lambda x_t^2$ with $\lambda = 0.048$
 - But Woodford studied a small calibrated model what goes in an estimated empirically realistic model?

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- Results hold up when allowing for realistic measurement errors in the output gap, and when we introduce interest rate smoothing to capture the observed gradualism in policy behavior
- Given the similarity of parameters and shocks in estimated models of other advanced economies, our results should be relevant for other CBs (e.g. ECB)

- Our exercise
- Model environment
- Benchmark results
- Robustness of results
- Concluding remarks

Our Exercise Quadratic approximation of utility and Ramsey policy

$$\sum_{t=0}^{\infty} \mathsf{E}_0\left[\beta^t U(X_t)\right] \simeq \textit{constant} - \sum_{t=0}^{\infty} \mathsf{E}_0\left[\beta^t X_t' W^{\textit{society}} X_t\right], \qquad (1)$$

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• Benigno and Woodford (2006) demonstrated that households utility function could be written as:

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- We adopt unconditional expectations operator for welfare evaluation, so the loss under Ramsey optimal policy is

$$Loss^{Ramsey} = \mathsf{E}\left[\left(X_{t}^{Ramsey}\left(W^{society}\right)\right)'W^{society}\left(X_{t}^{Ramsey}\left(W^{society}\right)\right)\right]$$

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• Measure welfare costs by comparing loss under mandate with Ramsey:

$$\mathsf{CEV} = 100 \left(\frac{Loss^{obj} - Loss^{Ramsey}}{\tilde{\mathcal{C}} \left(\frac{\partial U}{\partial \mathcal{C}} |_{s.s.} \right)} \right), \tag{3}$$

where $\bar{C}(\partial U/\partial C)$ measures how welfare increases when consumption is increased 1%

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• Hence, CEV is increase in SS C that make households in expectation equally well-off under simple mandate as under Ramsey policy

Key features of model structure

- Both EHL and SW models features monopolistic competition in both goods and labour markets
- Nominal price and wage stickiness:
 - Calvo price contracts, indexation of non-optimizers $P_t^{NO} = \Pi_{t-1}^{l_p} \Pi^{1-\iota_p} P_{t-1}^{NO}$
 - Calvo wage contracts, indexation of non-optimizers $W_t^{NO} = \gamma \Pi_{t-1}^{\iota_w} \Pi^{1-\iota_w} W_{t-1}^{NO}$
- SW model also features real rigidities as in CEE (2005):
 - External habit persistence in consumption
 - CEE type of investment adjustment costs
 - Variable capital utilization
 - Kimball (1995) aggregator; lower slope of price and wage schedules for given Calvo parameter

- Total factor productivity (ε_t^a) shocks that affect potential output.
- Two "inefficient" shocks (do not affect y_t^{pot}):
 - ε_t^p "price markup" shock
 - ε_t^w "wage markup" shock
 - Pay particular attention to what extent the two cost-push shocks drive our results
- SW also includes three additional structural shocks; Investment-specific (ε_t^i) , Risk-shock on financial assets (ε_t^b) , Government-NX (ε_t^g)

Parameters adopted from Smets and Wouters

- We use the posterior mode parameters from SW07 (Tables 1.A-B in their paper)
- Make assumptions on adjustment functions and how we introduce the shocks so that linearized representation of our model coincides exactly with SW07
• The Erceg, Henderson and Levin (2000) model similar to SW model, but omits physical capital and habit formation in consumer preferences. Key equations:

$$\pi_t^p = \beta \mathsf{E}_t \pi_{t+1}^p + \kappa_p y_t^{gap} + \vartheta_p \omega_t^{gap}, \qquad (4)$$

$$\pi_t^\omega = \beta \mathsf{E}_t \pi_{t+1}^\omega + \kappa_w y_t^{gap} - \vartheta_w \omega_t^{gap}, \qquad (5)$$

$$\omega_t^{gap} \equiv \omega_{t-1}^{gap} + \pi_t^\omega - \pi_t^p - \Delta \omega_t^n. \qquad (6)$$

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- Not possible to simultaneously stabilize y_t^{gap} , π_t^p and π_t^w .
- Example, in response to changes in ω_t^n due to ε_t^a , perfect stabilization of the output gap y_t^{gap} requires a change in the real wage ω_t , and thus a change in either prices or nominal wages (or both). But π_t^p and π_t^w cannot change if both y_t^{gap} and ω_t^{gap} are unchanged.

• Quadratic approximation of the household utility functional gives the following true loss function:

$$L_{t}^{R} = -\frac{1}{2} \left[\left(\pi_{t}^{P} \right)^{2} + \lambda_{w}^{opt} \left(\pi_{t}^{w} \right)^{2} + \lambda_{y}^{opt} \left(y_{t}^{gap} \right)^{2} \right],$$
(7)

where
$$\lambda_{w}^{opt} \equiv \frac{\epsilon_{\omega}(1-\alpha)}{\epsilon_{p}} \frac{\vartheta_{p}}{\vartheta_{w}}$$
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• But, assume that the CB is assigned the following simple mandate,

$$\mathcal{L}_{t}^{CB} = -\frac{1}{2} \left[\left(\pi_{t}^{p} \right)^{2} + \lambda_{y} \left(y_{t}^{gap} \right)^{2} \right],$$
(8)

which does not include π_t^w .

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- This equation implies that perfectly stabilizing y_t^{gap} leads to perfect stabilization of $\vartheta_w \pi_t^p + \vartheta_p \pi_t^\omega$, where a higher weight is attached to the inflation rate for which nominal rigidities are most severe.
 - Thus, stabilizing y_t^{gap} mitigates the welfare costs of nominal rigidities in both goods and labor markets.

Benchmark results in SW Model

Results for standard inflation-output mandate

• We start with a standard inflation - output based function

$$L_t = \left(\pi_t^a - \pi^a\right)^2 + \lambda^a x_t^2$$

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- CEV as function for λ^a for the alternate x_t measures are reported in Figure 1

CEV for simple mandates with alternative utilization measures



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Volatility trade-offs for alternative utilization measures



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Drivers of our results

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- Are the shocks or deep parameters driving our results?

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- Hence, we complement it by studying the influence of dynamic indexation and cost-push shocks

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- Turning to the cost-push shocks, we find that λ^a above or close to unity even when *either* var(ε^p_t) or var(ε^w_t) is set to nil
- However, when *BOTH* var (ε_t^p) or var (ε_t^w) are set to nil, then trade-off largely vanishes and λ^a is essentially irrelevant, but high weight still optimal

Sensitivity of results w.r.t. parameters and shocks



Variance frontiers for alternative calibrations



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- In contrast, JPT (2013) find that the output gap can be stabilized without generating higher inflation volatility
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Drivers of our results

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- While we do not neccessarily disagree with JPT, their "no trade-off" result is a special case in the sense that it applies only if *BOTH* price and wage markup shocks are irrelevant
 - And since we do not know if this is the case, robustness argument calls for large λ^a in actual policy communication

Robustness of results

 Importantly, we find that our results hold up when we put restrictions on std(r^a_t):

Results for loss function with interest rate term

Loss Function	$\lambda^a - y_t^{gap}$	λ_r	CEV (%)	$\operatorname{std}(r_t^a)$
Woodford	0.048	—	0.471	8.92
Optimized	1.042	_	0.044	9.00
Optimized*: $r_t^a - r^a$	1.161	0.0770*	0.076	2.24
Optimized*: Δr_t^a	1.110	1.0000^{*}	0.084	2.04

- Obviously, commitment assumption important here
- Results also hold up when we assume output gap measured with errors in real time

• Also study the merits of an alternative mandate with nominal wage inflation and a labor market gap $(I_t - I_t^{pot})$:

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$$L_{t} = \left(\Delta w_{t}^{a} - \Delta w^{a}\right)^{2} + \lambda^{a} \left(I_{t} - I_{t}^{pot}\right)^{2}$$

• Find that labor market variables may warrant further attention; not surprising given that the model features labor market frictions (nominal wage frictions)

Robustness of results

On the importance of labor market variables



DKLN (UPF, KU, Riksbank & Boston Fed)

On the Design of Simple Mandates

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- Our results warrant further work to check robustness in models with financial frictions, expectations formation, imperfect information, and plausible transmission lags of monetary policy